

Continuous Hydrogenation of 2-Butyne-1,4-diol to 2-Butene- and Butane-1,4-diols

C. V. Rode,* P. R. Tayade, J. M. Nadgeri, R. Jaganathan, and R. V. Chaudhari

Homogeneous Catalysis Division, National Chemical Laboratory, Dr. Homi Bhabha Road, Pune - 411008, India

Abstract:

Continuous catalytic hydrogenation of 2-butyne-1,4-diol (B₃D) was carried out in a fixed-bed reactor over 1% Pt/CaCO₃ catalyst to give 2-butene-1,4-diol (B₂D) and butane-1,4-diol (B₁D) without formation of any other side products. In case of continuous hydrogenation, higher selectivity (66%) to B₂D could be obtained and the selectivity pattern was completely different from that found in case of batch slurry operation in which B₁D selectivity was very much higher (83%) than the B₂D selectivity (17%). Another interesting feature was that by varying the contact time, the selectivity to both B₂D as well as B₁D could be varied over a wide range which is an attractive option to obtain the desired products mix of B₁D and B₂D, depending on the fluctuation in the market demand. Further, a mathematical model for reactor performance was also developed on the basis of the kinetic data obtained previously in a batch slurry reactor. The predicted values of conversion, selectivity, and rate of hydrogenation were found to agree with the experimental data over a wide range of conditions.

Introduction

Hydrogenation B₃D in the presence of a catalyst is an industrially important reaction for the manufacture of B₂D and B₁D.¹ The olefinic diol, B₂D, is a starting material for the manufacture of endosulfan and vitamins A and B₆, whereas B₁D has a wide range of applications in the polymer industry and as a raw material for the manufacture of tetrahydrofuran.^{1–3} The earlier processes described Ni- and Cu-based catalysts for butyne diol hydrogenation under severe operating conditions (15–30 MPa H₂ pressure and up to 433 K temperature).⁴ The noble metals such as palladium, ruthenium alone or in combination with other metals such as zinc, lead, cadmium, copper, and/or organic amines also were used as catalyst systems to improve selectivity (ratio of concentration of desired product formed to the concentration of substrate consumed) to the intermediate, B₂D.^{1,5–8} A monometallic Pd/C catalyst was reported to

give 60–70% selectivity to B₂D while remaining is a mixture of saturated diol (B₁D) along with other side products such as γ -hydroxy butyraldehyde, *n*-butyraldehyde, *n*-butanol, crotyl alcohol, and acetal due to the double bond migration and hydrogenolysis of B₂D in the presence of a catalyst.^{4,5} It is clear from the literature that, for butyne diol hydrogenation, a monometallic catalyst system gives saturated diol (B₁D) as major product along with other side products, whereas a combination of two or more metals or the presence of organic/inorganic bases gives enhanced selectivity to B₂D; however, such catalyst systems lack consistency in activity in subsequent catalyst reuse, and moreover, such processes require the complete removal of the additives for obtaining highest purity of the product for its end use in the fine chemical or pharmaceutical sector. Also, previous work on butynediol hydrogenation has mainly been carried out in a batch slurry reactor using finely powdered catalyst in which the selectivity ratio of B₂D to B₁D is normally constant. Since both B₂D and B₁D are large-scale commercial products, it would be most desirable to have a continuous hydrogenation of B₃D to give either B₂D or B₁D selectively or a desired mixture of B₂D and B₁D. As per the market demand, this continuous operation for the hydrogenation of B₃D by merely changing the operating conditions can give a desired mixture of B₂D and B₁D (Figure 8) for the same catalyst. Hence, objectives of this work were (i) to investigate the activity and selectivity of 1%Pt/CaCO₃ catalyst for continuous hydrogenation of butyne diol in a fixed-bed reactor, (ii) to study the effect of various reaction parameters on the conversion and selectivity behaviour for the continuous hydrogenation of B₃D, and (iii) to develop a reactor model that provides reasonably accurate conversion and selectivity predictions for various reactor inlet conditions. For this purpose, hydrogenation of butyne diol was carried out in a tubular reactor (30 g capacity); we found that the selectivity pattern obtained in a fixed-bed reactor was different from that obtained in the slurry reactor at similar conversion levels and that the selectivity ratio of B₁D to B₂D could be altered by varying the H₂ pressure, temperature, liquid and gas flow rate conditions at the reactor inlet. The predictions obtained by the proposed reactor model were compared with the experimental data and were found to agree well over a wide range of operating conditions.

Experimental Section

Materials. B₃D of >99.5% purity was obtained from E.Merck India, Ltd., and 10% aqueous solution was used.

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* To whom correspondence should be addressed. Fax: +91 20 25893260. E-mail: cv.rode@ncl.res.in.

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Table 2. Activity and selectivity pattern for butyne diol hydrogenation in a fixed-bed reactor

sr. no.	W/F (h)	conversion (%)	selectivity %	
			B ₁ D	B ₂ D
1	0.33	14	34	66
2	0.50	30	42	58
3	0.66	40	49	51
4	1.11	55	59	41
5	2	78	73	27

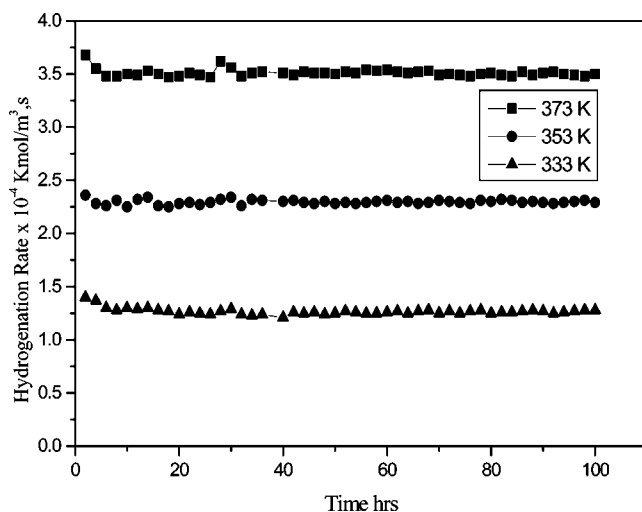


Figure 2. Time on stream catalyst activity profile. Reaction conditions: pressure, 20 bar; gas flow rate, 20 L/h; liquid flow rate, 20 mL/h; catalyst weight, 20 g.

loading to the liquid flow rate (W/F , h). Obviously, the conversion of B₃D increased with increase in contact time. The selectivity pattern was completely different from that found in case of batch slurry operation in which B₁D selectivity was very much higher (83%) than the B₂D selectivity (17%).⁹ As can be seen from Table 2, varying the contact time at different conversion levels could vary the selectivity to both B₂D as well as B₁D over a wide range. This is an attractive option for a commercial operation where the desired products mix of B₁D and B₂D can be achieved, depending on the fluctuation in the market demand.

Some preliminary experiments showed that the activity of 1%Pt/CaCO₃ for the hydrogenation of B₃D was constant for >100 h in the temperature range of 333–373 K (Figure 2), confirming the uniform activity for the duration of all experiments carried out in this work. Therefore, all of the data collected for the purpose of reactor modeling and reactor performance studies were under steady-state conditions.

Effect of Liquid Flow Rate. The effect of liquid flow rate on conversion of B₃D was studied in the range of 10–60 mL/h, under constant temperature, H₂ pressure, and gas flow rate conditions, and the results are shown in Figures 3 and 4. The conversion of B₃D decreased almost proportionately (from 70 to 12%) with increase in liquid flow rate from 10 to 60 mL/h (see Figure 3). One of the main reasons for decrease in the conversion is that, as the liquid flow rate

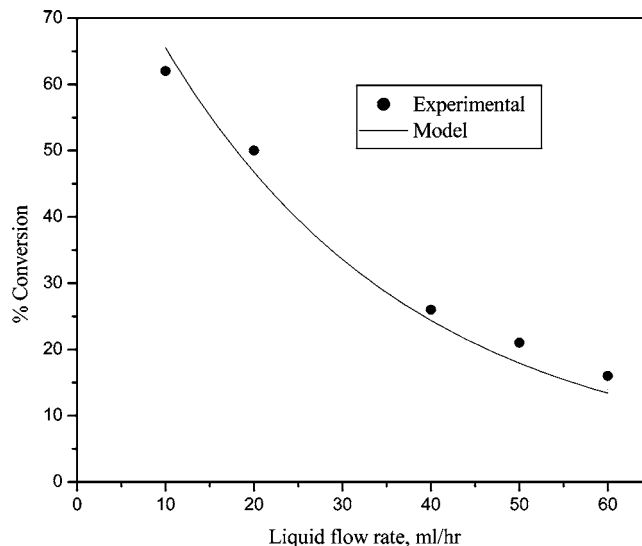


Figure 3. Effect of liquid flow rate on conversion. Reaction conditions: p_{H_2} , 20 bar; H₂ flow rate, 20 L/h; temperature, 100 °C; catalyst weight, 10 g.

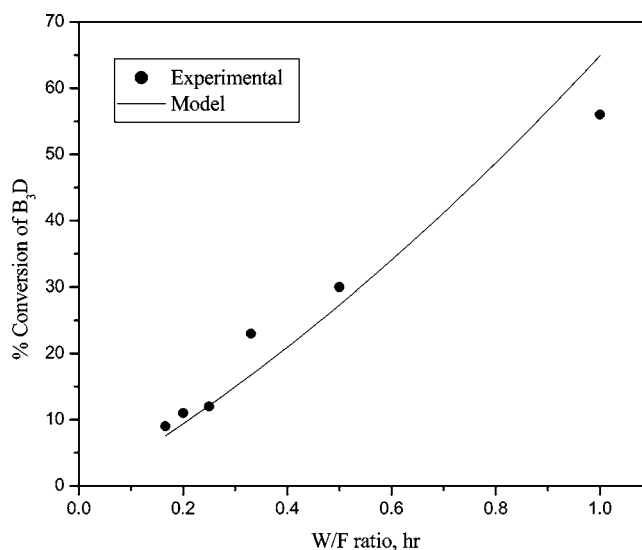


Figure 4. Effect of liquid flow rate on conversion. Reaction conditions: pressure, 20 bar; H₂ flow rate, 20 L/h; temperature, 100 °C; catalyst weight, 20 g.

was increased, the residence time of B₃D in the reactor was reduced and less time was available for the intimate contact of H₂ with liquid B₃D and with the catalyst pellets; thus, proper diffusion was not possible. Another reason is that, although the increase in the liquid flow rate could wet more surface area of catalyst pellets and there was an increase in the gas–liquid and liquid–solid mass transfer coefficient, at lower liquid velocity, catalyst particles were partially wetted; under these conditions the rate would increase due to direct transfer of the gas-phase reactant to the catalyst surface (already wetted internally due to capillary forces). Hence, with an increase in the liquid flow rate, an increase in the wetted fraction was expected to retard the rate of reaction.^{10,11} The overall rate of hydrogenation (Figure 5) decreased with increase in the liquid flow rate. In the range of 10–25 mL/h liquid flow rate, the fall in the rate is fast, and eventually it becomes slower. The model predictions for the effect of liquid flow rate on the conversion and overall

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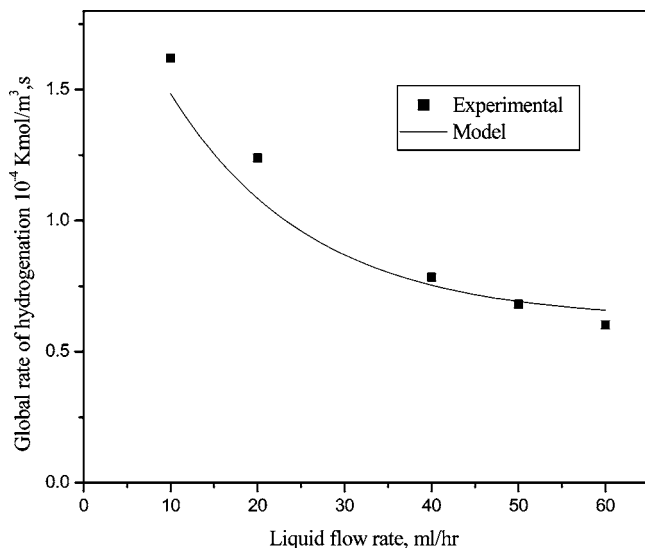


Figure 5. Effect of liquid flow rate on rate of hydrogenation. Reaction conditions: pressure, 20 bar; H₂ flow rate, 20 L/h; temperature, 100 °C; catalyst weight, 20 g.

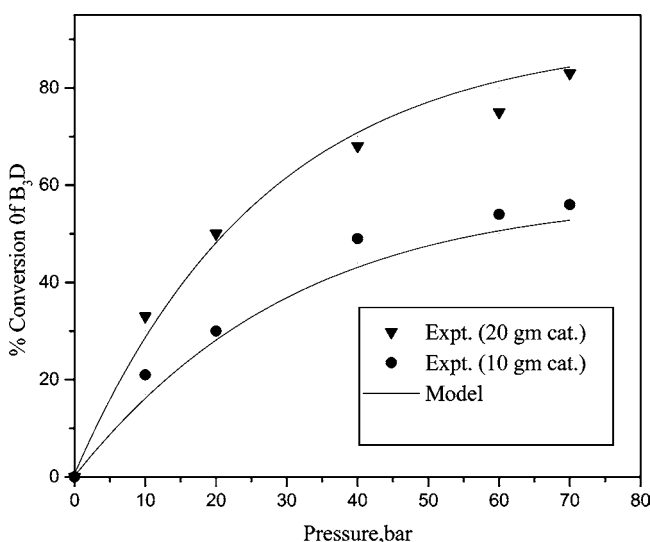


Figure 6. Effect of H₂ pressure on conversion. Reaction conditions: liquid flow rate, 20 mL/h; H₂ flow rate, 20 L/h; temperature, 100 °C.

rate of hydrogenation are in well agreement with the experimental results (see Figures 3 and 5).

Effect of H₂ Pressure. The effect of hydrogen pressure on the conversion of B₃D was studied in the range of 10–70 bar H₂ pressure for 10 and 20 g of catalyst loadings and at 100 °C, and the results are shown in the Figure 6. Initially, B₃D conversion increased almost linearly with increase in pressure up to 40 bar H₂ pressure. The overall rate of hydrogenation was also found to increase with increase in H₂ pressure (Figure 7) for both the catalyst loadings. The increase in H₂ pressure increases the gas–liquid and liquid–solid mass transfer coefficient, leading to higher conversion and hydrogenation rates. It was interesting to note that with increase in H₂ pressure, the selectivity patterns of B₂D and

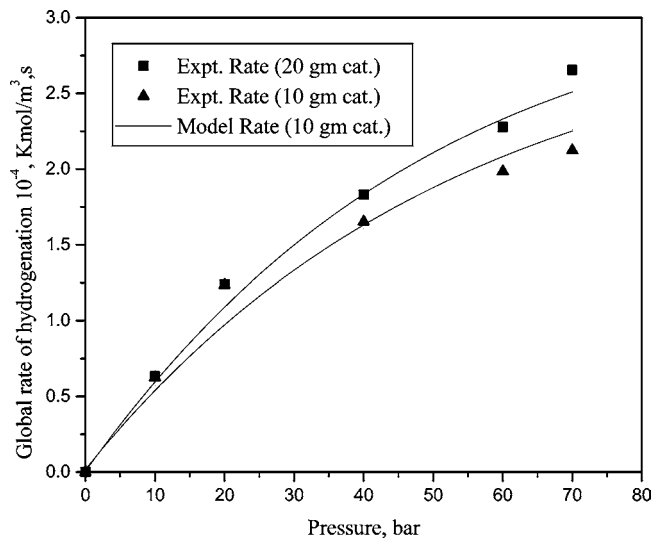


Figure 7. Effect of hydrogen pressure on rate of hydrogenation. Reaction conditions: liquid flow rate, 20 mL/h; H₂ flow rate, 20 L/h; temperature, 100 °C.

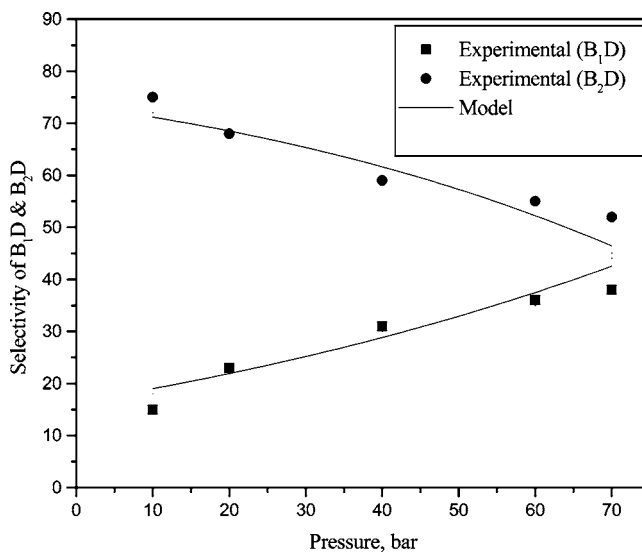


Figure 8. Effect of hydrogen pressure on the selectivity of B₂D and B₁D. Reaction conditions: liquid flow rate, 20 mL/h; catalyst weight, 20 g; H₂ flow rate, 20 L/h.

B₁D were exactly opposite to each other (see Figure 8). In the lower range of H₂ pressure (10–40 bar), the difference between the selectivities of B₂D and B₁D was larger; eventually, 50:50 formation of B₂D and B₁D could be obtained at 70 bar H₂ pressure. The predictions of the model equations for the effect of pressure on the conversion of B₃D, selectivity of B₂D and B₁D, and overall rate of hydrogenation is in good agreement with the experimental results.

Effect of Hydrogen Flow Rate. The effect of hydrogen gas flow rate on conversion of B₃D and selectivities of B₂D and B₁D were studied in the range of 20–80 L/h at constant pressure, temperature, and liquid flow rate conditions. The conversion of B₃D was slightly lower at the lower and higher gas flow rates as compared with that in the middle range (Figure 9). The reason for this situation is that at lower gas flow rate the gas cannot overcome the gas–liquid mass transfer resistance, while at higher gas flow rates, although the gas reduces the liquid film thickness around the catalyst

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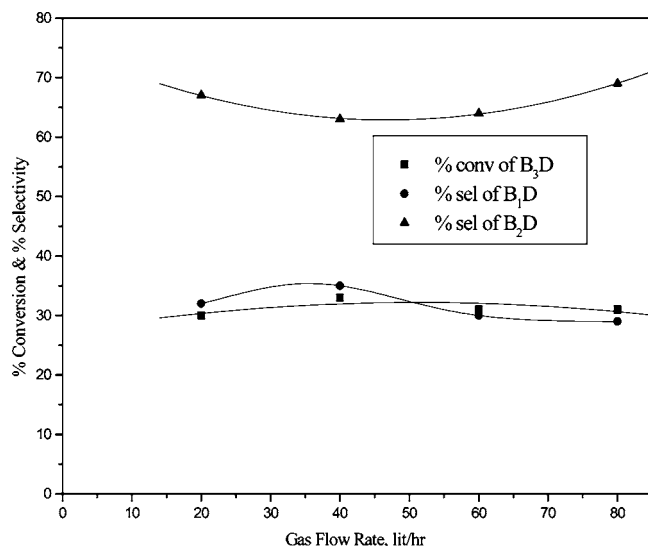


Figure 9. Effect of gas flow rate on conversion of B₃D. Reaction conditions: liquid flow rate, 20 mL/h; H₂ pressure, 20 bar; temperature, 100 °C; catalyst weight, 10 g.

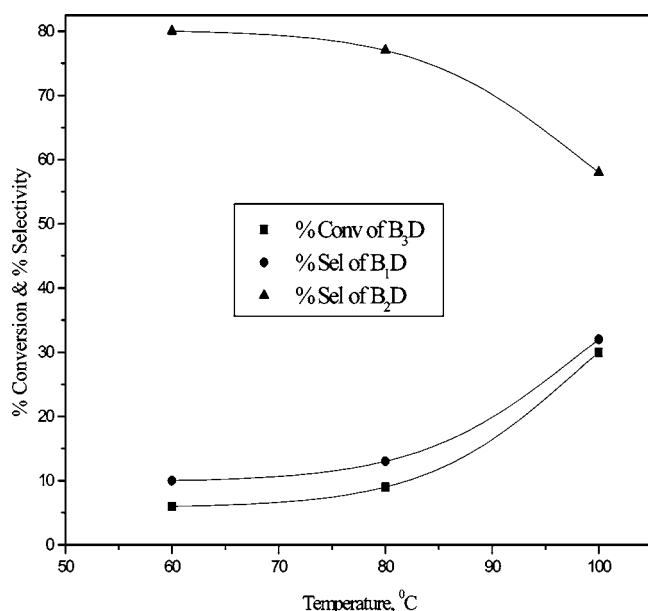


Figure 10. Effect of temperature on conversion of B₃D and selectivity of B₁D and B₂D. Reaction conditions: liquid flow rate, 20 mL/h; H₂ flow rate, 20 L/h; pressure, 20 bar; catalyst weight, 10 g.

pellets, the gas phase becomes continuous, and the liquid phase becomes dispersed. With further increase in gas flow rate, the flow regime changes to spray flow regime, and this causes greater velocities in the liquid phase by increasing the drag forces on the liquid phase. The selectivities to both B₂D and B₁D were nearly constant since the change in gas flow rate did not affect the intrinsic reaction kinetics to a considerable extent.

Effect of Temperature. The effect of temperature on conversion of B₃D and selectivity patterns of B₂D and B₁D were studied by varying the temperature from 60 to 100 °C (Figure 10). The conversion increased from 5 to 30% with increase in temperature from 60 to 100 °C since, the temperature has a greater impact on the reaction kinetics. The selectivity patterns of B₁D and B₂D showed opposite trends

Table 3. Kinetic parameters for the hydrogenation of B₃D

temp (K)	rate constants ($(\text{m}^3)^2/\text{kmol kg}\cdot\text{s}$)		adsorption constants (kmol/m^3)	
	k_1	k_2	K_B	K_C
333	1.940	1.210	8.101	2.11
343	3.178	2.790	9.80	2.60
353	5.037	6.140	11.728	3.183
363	7.802	12.934	13.898	3.843
373	11.804	26.178	16.32	4.594

with an increase in temperature, obviously because at higher temperature B₂D gets converted to the saturated diol B₁D.

Reactor Modeling. A trickle-bed reactor model for the hydrogenation of B₃D was developed using the rate equations proposed by Telkar et al. based on the rate data in a slurry reactor to represent the intrinsic kinetics for different reaction steps as shown in Scheme 1.⁹

$$r_1 = \frac{wk_1A^*B_1}{(1 + K_B B_1 + K_C C_1)^2} \quad (1)$$

$$r_2 = \frac{wk_2A^*C_1}{(1 + K_B B_1 + K_C C_1)^2} \quad (2)$$

The overall rate of hydrogenation can be given as

$$R_A = \frac{wk_1A^*(B_1 + k_2C_1)}{(1 + K_B B_1 + K_C C_1)^2} \quad (3)$$

where A, B₁, and, C₁ represent the concentrations of H₂, B₂D, and B₁D. A nonlinear least-squares regression analysis was used to obtain the values of the kinetic parameters in the above rate equation. For this purpose an optimization program based on the Marquardt's method¹² was used. The different kinetic parameter values evaluated for the above rate equation are given in Table 3.

To develop a trickle-bed reactor model applicable to hydrogenation of B₃D, the approximate solution of the catalytic effectiveness factor was performed for partial wetting of catalyst particles.¹³ The overall catalyst effectiveness factor could be expressed as a sum of the weighted average of the effectiveness factor in the dynamic liquid-covered, stagnant liquid-covered and complete gas-covered zones and with the assumptions that (a) gas and liquid phases are in plug flow; (b) the liquid-phase reactant is nonvolatile and was in excess as compared to the gaseous reactant; (c) the gas-liquid, liquid-solid, and intraparticle mass transfer resistances for H₂ are considered, whereas the liquid-solid and intraparticle mass transfer resistances for the liquid phase were negligible; (d) the interphase and intraparticle heat transfer resistances were negligible. The catalyst effectiveness factor equation for the hydrogenation of B₃D could be developed on the basis of the approaches already reported in the literature.^{14,15} Under the conditions of significant

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intraparticle gradient for the gas-phase reactant (H₂) and when the liquid-phase reactant was in excess, the overall rate of hydrogenation of B₃D was given as

$$R_A = \frac{\eta_C w k_1 A^* (B_1 + k_{21} C_1)}{(1 + K_B B_1 + K_c c)^2} \quad (4)$$

where η_C , the overall effectiveness factor for the spherical catalyst particle was given as

$$\eta_C = \frac{1}{\phi} \left(\coth 3\phi - \frac{1}{3\phi} \right) \quad (5)$$

ϕ is the Thiele parameter, and final dimensionless parameters are given in Appendix 1. For calculating ϕ , the values of effective diffusivity were estimated using the standard correlation.^{15,16} Various correlations used to calculate the different coefficients in this work are given in Appendix 1. The saturation solubility of hydrogen was calculated as

$$(A^*)_T = [P - (P_v)_T](H_c)_T \quad (6)$$

where, P_v is the vapor pressure of solvent.

At steady-state conditions, the sum of the convection term and the gas–liquid mass transfer term were in equilibrium with the liquid–solid mass transfer term in the dynamic zone and the volumetric mass exchange between the dynamic and stagnant zone. The final mass balance equations in dimensionless form for species A (H₂) are given as

$$\frac{da_{1d}}{dz} = \alpha_{gl}(1 - a_{1d}) - \frac{\eta_C \alpha_r (b_1 + k_{21} c_1)}{(1 + b_1 k_b + c_1 k_c)^2} x \left\{ \begin{array}{l} \frac{f_d a_{1d}}{(1 + \eta_C \phi^2 / N_d)} + \\ \frac{f_s a_{1d}}{(1 + \eta_C \phi^2 / N_s + \eta_C \phi^2 / \alpha_s N_s)} \end{array} \right\} \quad (7)$$

Similarly, the mass balance of liquid-phase reactant/products in dimensionless form can be given as

$$\frac{db_{1d}}{dz} = - \frac{\eta_C \alpha_r b_1 \chi}{q_B (1 + b_1 k_b + c_1 k_c)^2} \quad (8)$$

This equation represents the change in the concentration of B₃D in liquid phase in terms of dimensionless parameters.

$$\frac{dc_{1d}}{dz} = \frac{\eta_C \alpha_r (b_1 - k_{21} c_1) \chi}{q_B (1 + b_1 k_b + c_1 k_c)^2} \quad (9)$$

This equation represents the change in the concentration of

B₂D in liquid phase in terms of dimensionless parameters.

$$\frac{dp_{1d}}{dz} = \frac{\eta_C \alpha_r k_{21} c_1 \chi}{q_B (1 + b_1 k_b + c_1 k_c)^2} \quad (10)$$

This equation represents the change in the concentration of B₁D in liquid phase in terms of dimensionless parameters, where

$$\chi = \left\{ \frac{f_d a_{1d}}{(1 + \eta_C \phi^2 / N_d)} + \frac{f_s a_{1d}}{(1 + \eta_C \phi^2 / N_s + \eta_C \phi^2 / \alpha_s N_s)} + \frac{(1 - f_d - f_s) a_{1d}}{(1 + \eta_C \phi^2 / N_g)} \right\} \quad (11)$$

A program code in Q-Basic was developed to get the output of eqs 7–10. These equations were solved using a fourth-order Runge–Kutta method with the following initial conditions:

$$\text{At } z = 0, \quad a_1 = b_1 = 1; \quad c_1 = P_1 = 0 \quad (12)$$

The model equations developed above, allowed the prediction of concentrations of products/reactants along the length of the reactor. At any given length of the reactor the fractional conversion of B₃D (X_B) could be given as

$$X_B = 1 - b_1 \quad (13)$$

The overall rate of hydrogenation was calculated as

$$R_A = \frac{U_1}{L} (C_1 + 2 P_1) \quad (14)$$

Here U_1 , is the liquid velocity in m/s, L is the length of the catalyst bed in m, C_1 , P_1 are the concentrations of B₂D and B₁D, respectively. The selectivities of B₂D and B₁D were calculated as

$$S_{B_2D} = \frac{c_1}{(1 - b_1)} \times 100 \quad (15)$$

$$S_{B_1D} = \frac{P_1}{(1 - b_1)} \times 100 \quad (16)$$

The applicability of the model was verified by comparing the predicted concentration vs time profiles as well as conversion of B₃D and selectivities to B₂D and B₁D with the experimental results under various inlet conditions. These results have already been discussed above and are shown in Figures 5–8, which showed an excellent agreement between the predicted values and the experimental data.

Conclusions

Hydrogenation of 2-butyne-1,4-diol (B₃D) was carried out using 1% Pt/CaCO₃ catalyst in a fixed-bed reactor. This process represents a consecutive reaction scheme giving 2-butene-1,4- and butane-1,4-diols. In a continuous hydrogenation process, the ratio of butene- and butane diols could be manipulated by tailoring the operating conditions for the same catalyst. The liquid flow rate and pressure of the hydrogen gas showed a significant effect on the conversion

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of B₃D and overall rate of hydrogenation. A theoretical model was also developed incorporating the conditions of external and intraparticle mass transfer, partial wetting of the catalyst and reaction kinetics of butyne diol hydrogenation in a batch slurry reactor. The reactor model was validated by carrying out hydrogenation experiments under various reactor inlet conditions, and model predictions were found to agree well with the observed conversion, selectivity data.

NOTATION

a_l	concentration of hydrogen in liquid phase, (= A_l/A^*), dimensionless
a_s	concentration of hydrogen on the catalyst surface, (= A_s/A^*), dimensionless
a_p	external surface area of the pellet [= $6(1 - \epsilon_b)/d_p$], m^{-1}
a_t	packing external surface area per unit volume of the reactor [= $S_{ex}(1 - \epsilon_b)/V_B$]
a_w	catalyst area wetted, m^{-1}
A_l	concentration of hydrogen in liquid phase, $kmol/m^3$
A_s	concentration of hydrogen on the catalyst surface, $kmol/m^3$
A^*	concentration of hydrogen in equilibrium with liquid, $kmol/m^3$
b_l	concentration of B ₃ D in liquid phase (= B_l/B_{li}), dimensionless
B_l	concentration of B ₃ D in liquid phase, $kmol/m^3$
B_{li}	initial concentration of B ₃ D in liquid phase, $kmol/m^3$
c_l	concentration of B ₂ D in liquid phase, (= C_l/B_{li}), dimensionless
C_l	concentration of B ₂ D in liquid phase, $kmol/m^3$
D_e	effective diffusivity, m^2/s
D_M	molecular diffusivity, m^2/s
d_p	particle diameter, m
f_d	fraction of catalyst wetted by dynamic liquid
f_s	fraction of catalyst wetted by the stagnant liquid
f_w	wetted fraction
F	liquid flow rate, kg/h
k_1, k_2	reaction rate constants, (m^3/kg) ($m^3/kmol \cdot s$)
k_{21}	dimensionless rate constant (= k_2/k_1)
k_b, k_c	dimensionless equilibrium constant ($k_b = K_B B_{li}$; $k_c = K_C B_{li}$)
k_s	liquid–solid mass transfer coefficient, $m s^{-1}$
k_{gs}	gas–particle mass transfer coefficient, $m s^{-1}$
K_A, K_B, K_C	adsorption constants, $m^3/kmol$
k_{lAB}	gas–liquid mass transfer coefficient, s^{-1}
K_{ex}	exchange coefficient between dynamic and stagnant liquid, s^{-1}
L	reactor length, m
N_d	Nusslet number for the liquid phase in the dynamic zone
N_s	Nusslet number for the liquid phase in the stagnant zone

N_g	Nusslet number for the gas phase
q_B	stoichiometric ratio (= B_{li}/A^*)
r_1, r_2	reaction rate for the individual hydrogenation steps, $kmol/m^3/s$
R	radius of the pellet, m
R_A	overall rate of hydrogenation, $kmol/m^3/s$
Re_l	Reynolds number for the liquid phase
S_{ex}	external surface area of the catalyst pellet, m^2
U_g	gas velocity (superficial), m/s
U_l	liquid velocity (superficial), m/s
W	weight of catalyst, kg/m^3
Z	reactor length, m

Greek letters

α_{gl}	dimensionless gas–liquid mass transfer coefficient
α_{ls}	dimensionless liquid–solid mass transfer coefficient
α_r	dimensionless reaction rate constant
ϵ	porosity of catalyst
ϵ_b	bed voidage

Appendix 1

(1) Dimensionless parameters used in the model:

gas–liquid mass transfer	$a_g = k_l a_B L/U_1$
liquid–solid mass transfer	$a_{ls} = k_s a_p L/U_1$
gas–solid mass transfer	$a_{gs} = k_{gs} a_p L/U_1$
Nusslet no. in dynamic zone	$N_d = R k_{sd}/3 D_e$
Nusslet no. in stagnant zone	$N_s = R k_{ss}/3 D_e$
reaction rate constant	$\alpha_r = L w k_l b_l / U_1$
equilibrium constants	$k_{21} = k_2/k_1$; $k_b = K_B B_{li}$; $k_c = K_C B_{li}$
Thiele parameter	$\phi = \frac{R}{3} \left[\frac{S_p (k_1 B_l + k_2 C_l)}{D_e (1 + K_B B_l + K_C C_l)^2} \right]^{1/2}$

(2) Correlations used in this work:

parameter	author(s)	ref
molecular diffusivity	Wilke and Chang	16
gas–liquid mass transfer coefficient	Goto and Smith	18
liquid–solid mass transfer coefficient	Satterfield et al.(1978)	19
gas–particle mass transfer coefficient (value used)	Zheng Lu et al.	20
volumetric mass exchange coefficient	Hochmann and Effron	21
total liquid hold-up	Sato et al.	22
static liquid hold-up (value used)	Zai-sha Mao et al.	23
saturation solubility	Stephen and Stephen	24
wetting efficiency	Mills and Dudukovic	25

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